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EFFECT OF IONIC STRENGTH AND ION PAIRING ON SOUND ABSORPTION IN AQUEOUS SOLUTIONS OF  ${\rm MgSO}_{\Delta}$  AND NaC1

C. Neuberger, C. C. (Paul) Hsu and F. H. Fisher

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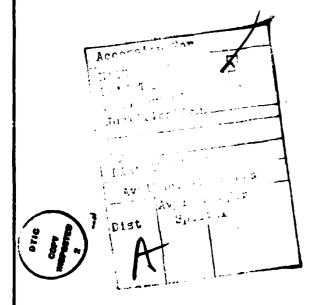
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Sound absorption in aqueous solutions of MgSO, is reduced by the addition of NaCl. From the Eigen and Tamm multistate dissociation theory it can be shown that the absorption exhibited by MgSO, is proportional to the ion-pair concentration. The reduction in sound absorption observed upon the addition of NaCl is treated theoretically and is attributed to two effects; formation of NaSO, and MgCl ion-pairs and an increase in ionic strength, both of which reduce the concentration of MgSO, ion pairs. Comparisons between theory and experiment support the theoretical treatment presented. For 0.02 molar

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MgSO, solutions with the addition of up to 0.12 molar NaCl, the theory is in good agreement with the data of Hsu and Fisher and in substantial conflict with the data in 0.017 molar MgSO, mixtures with NaCl of Kurtze and Tamm. For 0.1 and 0.17 molar MgSO, solutions, the data of Kurtze and Tamm are in better agreement with theory. The extension to high ionic strength of Debye-Huckel theory derived for low ionic strength is discussed briefly.



## EFFECT OF IONIC STRENGTH AND ION PAIRING ON SOUND ABSORPTION IN AQUEOUS SOLUTIONS OF MgSO<sub>4</sub> AND NaCl

C. Neuberger, C. C. Hsu and F. H. Fisher

#### **ABSTRACT**

Sound absorption in aqueous solutions of MgSO<sub>4</sub> is reduced by the addition of NaCl. From the Eigen and Tamm multistate dissociation theory it can be shown that the absorption exhibited by MgSO<sub>4</sub> is proportional to the ion-pair concentration. The reduction in sound absorption observed upon the addition of NaCl is treated theoretically and is attributed to two effects; formation of NaSO<sub>4</sub> and MgCl ion-pairs and an increase in ionic strength, both of which reduce the concentration of MgSO<sub>4</sub> ion pairs. Comparisons between theory and experiment support the theoretical treatment presented. For 0.02 molar MgSO<sub>4</sub> solutions with the addition of up to 0.12 molar NaCl, the theory is in good agreement with the data of Hsu and Fisher and in substantial conflict with the data in 0.017 molar MgSO<sub>4</sub> mixtures with NaCl of Kurtze and Tamm. For 0.1 and 0.17 molar MgSO<sub>4</sub> solutions, the data of Kurtze and Tamm are in better agreement with theory. The extension to high ionic strength of Debye-Huckel theory derived for low ionic strength is discussed briefly.

#### INTRODUCTION

Below 300 kHz sound absorption in low concentration aqueous  $MgSO_4$  solutions exceeds that due to pure water; for example, in a 0.02 molar solution at  $25^0$  the absorption due to a pressure dependent chemical relaxation exceeds the water value by a factor of 37 [1] at frequencies well below the 100 kHz relaxation frequency. When NaCl is added to  $MgSO_4$  solutions, the absorption due to  $MgSO_4$  is reduced substantially as Kurtze and Tamm [2] first demonstrated; for a ratio  $[NaCl]/[MgSO_4] = 5$ , their results indicated a reduction of half in absorption, independent of the initial  $MgSO_4$  concentration of 0.017, 0.1 and 0.17 moles/liter.

Kurtze and Tamm attributed the decrease in absorption to the reduction of MgSO<sub>4</sub> ion-pairs due to the formation of MgCl<sup>+</sup> and NaSO<sub>4</sub> ion-pairs. That the sound absorption in the mixture is due to MgSO<sub>4</sub> ion-pairs was shown both by Kurtze and Tamm and Wilson and Leonard [3] [4] since neither MgCl<sub>2</sub>, Na<sub>2</sub>SO<sub>4</sub> nor NaCl solution exhibit significant absorption below 300 kHz. These results have been discussed in the extensive review by Stuehr and Yeager [5] of acoustic research in electrolyte solutions. Recent work by Hsu and Fisher [6] found that a 0.03 M Na<sub>2</sub>SO<sub>4</sub> solution would exhibit the same absorption as that by pure water in the frequency range of 30-300 kHz. These results for Na<sub>2</sub>SO<sub>4</sub> are in agreement with data extrapolated from results obtained at higher frequencies and concentrations by Gilligan and Atkinson [7] in Na<sub>2</sub>SO<sub>4</sub> solutions.

Eigen, Kurtze and Tamm [8] attempted to account quantitatively for the observed reduction based on NaSO<sub>4</sub> ion-pairing; however, they used the same dissociation constant for NaSO<sub>4</sub> and MgSO<sub>4</sub>. Bies [9] attempted to account for the reduction on the basis of ionic strength effects on activity coefficients. In analyzing conductance data, Fisher [10] and Fisher and Fox [11] used the Kurtze and Tamm results in arguing for greater association in Na<sub>2</sub>SO<sub>4</sub> solutions, that is, a decrease in the dissociation constant of 0.19 reported by Jenkins and Monk [12] to a value of 0.10. Fisher and Fox [11] also reported dissociation constants for MgCl<sup>+</sup> ion pairing.

The purpose of this paper is to account for the reduction of sound absorption in MgSO<sub>4</sub>-NaCl mixtures on a theoretical basis, using the conductance results of Fisher and Fox [3] for MgCl and NaSO<sub>4</sub> ion pairing and the conductance results of Fisher and Fox [14] for MgSO<sub>4</sub> which are in close agreement with those of Pethybridge and Taba [15]. In this paper we make use of the same Debye-

Huckel (DH) equation for the activity coefficient as used in analyzing the conductance data [11] [16] [17]. We also apply the DH equation to higher ionic strength regions based on the fact that stoichiometric activity coefficients  $\gamma_{\pm} = \alpha f_{\pm}$  calculated for MgSO<sub>4</sub> solutions up to 1 molar very closely match the experimentally derived vapor pressure and freezing point values reported by Robinson and Jones [18], as well as the values derived from the equation by Lietzke and Stoughton [19].

From our analysis we find, contrary to the experimental results of Kurtze and Tamm, that the reduction in absorption does depend on the initial MgSO<sub>4</sub> concentration. While our theoretical results are in fair agreement with their high concentration results, we differ greatly with their results at low concentration. We suspect that their low concentration data, the most difficult region in which to make accurate measurements, contained substantial experimental errors. Recent acoustic results reported by Hsu and Fisher [1] for the addition of NaCl to 0.02 molar MgSO<sub>4</sub> solutions are in good agreement with the theoretical results presented in this paper.

#### 2. THEORY

Liebermann [20] was the first to show how sound absorption due to a pressure dependent chemical relaxation was related to the speciation and kinetics of the reaction. The absorption is expressed as follows:

$$\alpha(cm^{-1}) = \frac{\pi\beta_{ch}}{\beta_o C} \frac{f_r f^2}{f^2 + f_r^2}$$
 (1)

where  $\beta_{ch}$  is the chemical compressibility (cm<sup>2</sup>/dyne),  $\beta_o$  the isothermal compressibility (cm<sup>2</sup>/dyne), C the sound velocity (cm/sec), f, the relaxation frequency and f the acoustic frequency, both in Hz. For analysis of acoustic data in systems which demonstrate relaxation processes it is more convenient to analyze data and summarize results using the equation for absorption per wavelength:

$$\alpha \lambda = \frac{\pi \beta_{ch}}{\beta_0} \frac{f_r f}{f^2 + f_r^2} \tag{2}$$

as discussed by Stuehr and Yeager, for example, or  $Q\lambda$  used by Kurtze and Tamm where Q is absorption per molecule of solute:

$$Q\lambda = \frac{2\alpha\lambda}{cN^o} \tag{3}$$

where c is concentration in moles/liter and  $N^0$  is the Avogadro constant.

Eigen and Tamm, in their extensive theoretical work to explain the absorption data of Kurtze and Tamm in  $MgSO_4$  solutions over wide concentration (.02 to 0.2 mole/liter) and frequency ranges  $(10^4 - 10^8 \text{ Hz})$  postulated a multistate dissociation theory in which three species of ion pairs are involved as seen in Eq. 4:

$$Mg^{++} + SO_4^{--} \xrightarrow{k_{12}} MgOH_2H_2OSO_4 \xrightarrow{k_{23}} MgOH_2SO_4 \xrightarrow{k_{34}} Mg \xrightarrow{V_4} Mg \xrightarrow{S}O_4$$

$$Mg^{++} + SO_4^{--} \xrightarrow{k_{12}} MgOH_2H_2OSO_4 \xrightarrow{k_{23}} MgOH_2SO_4 \xrightarrow{m_3} Mg \xrightarrow{k_{43}} Mg \xrightarrow{Mg}O_4$$
(4)

where the  $V_i$  are the partial volumes (cc/mole) and the  $m_i$  are the concentrations in (moles/cc).

In the Eigen-Tamm normal-mode theory to explain the 100 kHz (primary relaxation per Stuehr and Yeager) and the 200-400 MHz relaxations, the chemical compressibility ( $\beta_{III}$ ) associated with the primary relaxation is shown below (using their notation).

$$\beta_{III} = \frac{(m_1' + m_2 + m_3)m_4}{m_1' + m_2 + m_3 + m_4} = \frac{(\Delta V_{III})^2}{RT},$$
 (5)

where  $m_1'$  is a concentration term including consideration of activity coefficients and  $\Delta V_{III}$  is a

normalized volume change consisting of a linear combination of the  $(V_i - V_{i+1})$  as in Eq. 4. From Eq. 5 it is seen that if  $m_4$  is a small fraction of the total ion pair concentration,  $m_4 << m_2 + m_3 + m_4$ , the chemical compressibility and therefore the absorption can be written as:

$$\beta_{III} = \frac{m_4 (\Delta V_{III})^2}{RT} \tag{6}$$

and 
$$\alpha\lambda = \frac{\pi m_4 \{\Delta V_{III}\}^2}{\beta^o RT} \frac{ff_r}{f^2 + f_r^2}$$
 (7)

Since  $m_4$  is directly proportional to the total ion-pair concentration, we see that sound absorption is therefore directly proportional to the total ion-pair concentration for a constant  $\Delta V_{III}$  and negligible changes in  $\beta_0$ .

The assumption that  $m_4$  is a small fraction of all the ion pairs is supported by measurements of the effect of pressure on conductance and absorption in MgSO<sub>4</sub> solutions [21] [22]. Briefly, for a change of 1000 atm, the ion-pair concentration decreases only by 10% whereas the absorption drops by a factor of three. This paradoxical behavior as discussed by Fisher and Fox [14], is consistent with the multistate dissociation model though exact agreement has yet to be achieved. Failure to obtain exact agreement does not diminish the multistate theory. That the agreement is as good as it is must be considered remarkable because The Eigen and Tamm multistate model, deduced to explain the ultrasonic spectrometry data of Kurtze and Tamm, was derived solely from atmospheric pressure data. Since absorption is proportional to the product of a concentration times the square of a volume change, a range of parameters for the equilibrium constants and  $\Delta V$  values were used by Eigen and Tamm in their multistate model,  $\pm 50\%$  for the equilibrium constants and  $\pm 20\%$  for the  $\Delta V$  terms. The set of values which best described both the acoustic and conductance data as a function of pressure indicated that  $m_4$  is only about 5% of the total ion pair concentration. This is the basis for the assumption that  $m_4 < < m_2 + m_3 + m_4$ , thereby justifying the use of Eqn. (7).

We proceed then on the basis that sound absorption in  $MgSO_4$ -NaCl mixtures is a measure of ion-pairing of  $MgSO_4$  since  $Na_2SO_4$ ,  $MgCl_2$  and NaCl solutions exhibit negligible absorption. Consequently, as NaCl is added to an  $MgSO_4$  solution a reduction in absorption is attributed to a decrease in ion pairing of  $MgSO_4$ . Fisher [23] applied this concept to sound absorption in sea water, using the absorption to deduce the concentration of  $MgSO_4$  ion-pairs in a complex mixed electrolyte solution at high ionic strength, I = 0.7, where the NaCl concentration is more than 10 times the concentration of the Mg or  $SO_4$  ions. The results for seawater were in good agreement with the theoretical modelling of Garrels and Thompson [24].

If we denote the neutral ion pair concentration for  $MgSO_4$  as  $[MgSO_4^0]$  we then write:

$$\frac{\{\beta_{III}\}_{M}}{\{\beta_{III}\}_{Q}} = \frac{\{m_{4}\}_{M}}{\{m_{4}\}_{Q}} = \frac{[MgSO_{4}^{2}]_{M}}{[MgSO_{4}^{2}]_{Q}}$$
(8)

for the mixture (M) and initial (O) pure solutions. Note that in Eq. (7) the maximum absorption per wavelength  $(\alpha\lambda)_{\max}$  occurs when  $f = f_{\Gamma}$  and that Eq. (8) can be rewritten as (assuming negligible change in  $\beta_o \, or \Delta \, V_{III}$ )

$$\frac{\{\alpha\lambda_{\max}\}_M}{\{\alpha\lambda_{\max}\}_O} = \frac{[MgSO_1^2]_M}{[MgSO_2^2]_O}.$$
(9)

#### 3. METHOD OF CALCULATION

The calculations to evaluate the right hand side of Eqn. (9) are relatively straightforward, requiring only the dissociation constants of 0.0062 [14], 0.1 [13] and 0.178 [13] for MgSO<sub>4</sub>, NaSO<sub>4</sub> and MgCl respectively. The Debye-Huckel equation [25] [26] [27]

$$-\log f_{ij} = A|z_i z_j| \frac{\sqrt{I}}{1 + Ba_{ij}\sqrt{I}} \tag{10}$$

is used to calculate the activity coefficients in the equations:

$$K_1 = \frac{[Mg^{++}] \{SO_4^{--}\} f_{22}^2}{[MgSO_4^2]}, \tag{11}$$

$$K_2 = \frac{[Na^+][SO_4^-]f_{12}f_{21}}{[NaSO_4]f_{11}},$$
(12)

$$K_3 = \frac{[Mg^{++}][Cl^-]f_{21}f_{12}}{[MgCl^+]f_{11}},\tag{13}$$

where the ionic strength  $I = 0.5 \Sigma C_i z_i^2$  which, of course, includes the charged ion pairs. Values for A and B are the usual Debye-Huckel values at  $25^{\circ}$  and the  $a_{ij}$  values are 11.58, 5.79 and 2.90 A for the 2-2, 1-2 or 2-1, and 1-1 activity coefficients. The  $a_{ij}$  value of 11.58 A is based on the results of Fisher and Fox [14] for MgSO<sub>4</sub> and we use the Bjerrum [28] idea of making the distance proportional to the product of the charges to get the other  $a_{ij}$  values.

The procedure is to solve the above equations (10)-(13) to determine the initial and final concentration of MgSO<sub>4</sub> in Eqn. (9) for pure MgSO<sub>4</sub> and the mixtures as NaCl is added.

Since there is an increase in ionic strength, some of the reduction in MgSO<sub>4</sub> will be due to ionic strength effects on the activity coefficient and the remainder will be due to ion-pairing effects. To separate these two effects we calculate the decrease in MgSO<sub>4</sub> ion pairs due to the increased ionic strength as if no NaSO<sub>4</sub> and MgCl<sup>+</sup> ion pairing occurred, but at the same ionic strength calculated using Eqns. (10)-(13) and the dissociation constants given above; the ionic strength effect, therefore, is calculated at the same ionic strength including all pairing. The remainder of the decrease in MgSO<sub>4</sub> is then attributed to ion-pairing effects. This artificial separation of the two effects provides insight into their relative significance.

In this work we have used Eqn. (10) over a wide range of ionic strengths, a procedure which is certainly open to challenge. However, since our analysis is on a differential basis, errors in absolute values of concentration will offset one another, and also free activity coefficients calculated with Eqn. (10) are consistent with the stoichiometric activity coefficients of Robinson and Jones. Therefore, the work reported here should be regarded as an initial step in making a critical evaluation of the relation between acoustic data and thermodynamic dissociation constants obtained from independent data.

#### 4. DISCUSSION OF RESULTS

The results of our calculations are shown partially in Table I and more completely in Fig. 1 in which we compare our results with the experimental data of Kurtze and Tamm. To facilitate numerical comparison of our results with those of Kurtze and Tamm we make use of the empirical formula they used to summarize their results:

$$\frac{A}{A_o} = \frac{[MgSO_4]}{[MgSO_4] + F[NaCl]},\tag{14}$$

where A is sound absorption in the MgSO<sub>4</sub>-NaCl mixture and A<sub>0</sub> is absorption in pure MgSO<sub>4</sub> solution. In the context of our theoretical treatment

$$\frac{A}{A_o} = \frac{[MgSO_1]_M}{[MgSO_2]_O} = \frac{\{\alpha\lambda\}_M}{\{\alpha\lambda\}_O}.$$
 (15)

If we rewrite Eq. (16) as follows:

$$\frac{A_o - A}{A} = F \frac{[NaCl]}{[MgSO_4]} = FR, \tag{16}$$

we then see how Fig. 1 relates the absorption data in terms of the intercept F for equal concentrations of NaCl and MgSO<sub>4</sub>. The greater the reduction in absorption whether due to ion-pairing or ionic strength effects, the greater value of F. Therefore, in the MgSO<sub>4</sub>-NaCl system, F is a measure of ion association for NaSO<sub>4</sub> and MgCl as well as of ionic strength.

Whereas Kurtze and Tamm experimentally arrived at the conclusion that F = 0.21, a constant independent of the initial concentration of  $MgSO_4$  our theoretical analysis indicate otherwise as seen in Fig. 1 and in Fig. 2. We may summarize our theoretical results for  $MgSO_4$ -MgCl units shown in Fig. 2 with the equation:

$$F \approx 0.32 \ c^{0.27} \tag{17}$$

where c (moles/liter) is the concentration of MgSO<sub>4</sub> or NaCl. Fig. 3 summarizes the ionic strength and ion-pairing effects for 0.017 M MgSO<sub>4</sub> solutions as NaCl is added.

While our high concentration calculations agree reasonably well with the experimental data of Kurtze and Tamm as seen in Fig. 1, the low concentration (0.017 molar) results do not. However, the lower  $MgSO_4$  concentration region is a more difficult one in which to make accurate measurements. Also, only two of the Kurtze and Tamm data points are for 0.017 M  $MgSO_4$ . Recent work by Hsu [1] for 0.02 molar  $MgSO_4$  aqueous solutions with values of R = 1, 2, 4 and 6 for the addition of NaCl yielded F = 0.129, in good agreement with the value of F = 0.134 calculated according to the theory in this paper and as shown numerically in Fig. 1. If the dissociation constants for  $NaSO_4$  and  $MgCl^+$  are doubled, we see in Table II that the theoretically derived value for F is outside the range of experimental error in the work reported by Hsu and Fisher [1]. Other variations of the theoretical calculations are shown in Table II, all of which provide support for the dissociation constants we used, namely, .0062, 0.1 and 0.178 for  $MgSO_4$ ,  $NaSO_4$  and  $MgCl^+$ , respectively. With further refinements it is felt that the experimental error can be reduced so that the acoustic data can provide a more accurate basis for analysis of dissociation constants.

Therefore, we have both experimental and theoretical results in fair agreement with one another at low concentrations and certainly both in disagreement with the low concentration results of Kurtze and Tamm. This initial theoretical effort to understand sound absorption in mixtures of MgSO<sub>4</sub> and NaCl is encouraging.

Questions arise about the use of the Debye-Huckel activity coefficient equation regarding its use in high ionic strength regions. It is therefore worthwhile to mention that stoichiometric activity coefficients for pure  $MgSO_4$  solutions calculated with our K=0.0062 are in close agreement with those reported by Robinson and Jones [18] and Lietzke and Stoughton [19] from experimental data as seen in Table III. Such agreement does not mean we are necessarily correct in our theoretical approach but only that we are not in gross disagreement with what is known. For pure  $MgSO_4$  solutions up to 0.1 molar the absorption data of Kurtze and Tamm are proportional to the ion-pair concentration calculated using Eqs. (10) and (11).

#### 5. CONCLUSION

In this work we have evaluated what to expect for sound absorption reduction in MgSO<sub>4</sub> solutions as NaCl is added, separating the effects of ionic strength and ion pairing. We find that in the empirical equation of Kurtze and Tamm, F is not independent of the concentration of MgSO<sub>4</sub>.

For  $0.02 \text{ M MgSO}_4$  solutions we calculate F = 0.134 which is in good agreement with the value F = 0.129 Hsu [1] obtained with recent acoustic measurements at the same MgSO<sub>4</sub> concentration.

Therefore, predictions for the reduction in sound absorption as NaCl is added to MgSO<sub>4</sub> solutions are in good agreement with acoustic data and provides independent support for the lower dissociation constant of NaSO<sub>4</sub> reported by Fisher and Fox.

The agreement with the higher concentration data of Kurtze and Tamm may be fortuitous in view of the limitations of using the Debye-Huckel activity coefficient equation as expressed in Eqn. (10) at

high ionic strengths. However, the differential basis of the calculations partially compensates for absolute errors in the concentration of MgSO<sub>4</sub> ion pairs. This work demonstrates in principle how sound absorption data can be used to study ion-pairing in mixed salt solutions on a quantitative basis. The agreement between the predicted and observed values of absorption in .02 M MgSO<sub>4</sub>-NaCl mixtures is encouraging.

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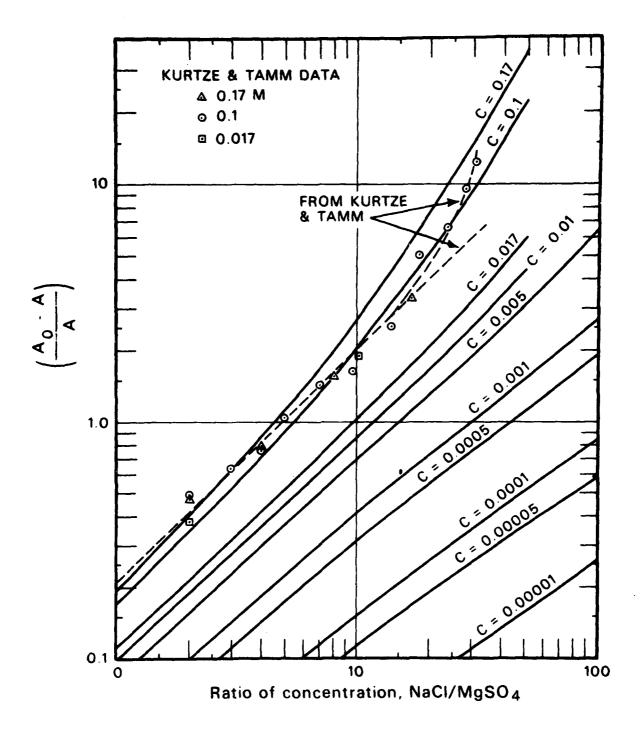


Fig. 1. Comparison of calculated and measured values of sound absorption reduction in MgSO<sub>4</sub> solutions as NaCl is added. Data points and dashed curves are from Kurtze and Tamm at 20°C. Solid curves are calculated values for each MgSO<sub>4</sub> concentration at 25°.

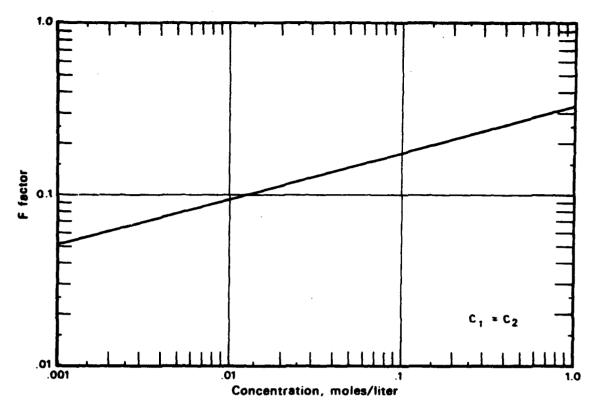


Fig. 2. Plot of F value for equal concentrations of  ${\rm MgSO_4}$  and  ${\rm NaCl}$  .

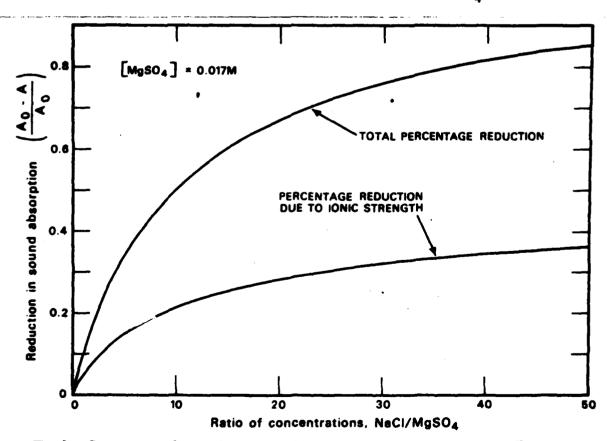


Fig. 3. Comparison of reduction in sound absorption due to ionic strength effects with total absorption for a  $0.017~M~MgSO_4$  solutions as NaCl is added.

TABLE I

Sound Absorption Reduction  $\Delta A$  at 25° in Mixtures of MgSO<sub>4</sub> and NaCl Aqueous Solutions and Ion-Pair Concentrations as a Function of MgSO<sub>4</sub> Concentration and Various [NaCl]/[MgSO<sub>4</sub>] Ratios, R

$[MgS0_4]_{o}$	R	(a)	(b)	(c)	(d)	ΔΑ	(e)	<b>(f)</b>
moles/l			x 10 <sup>4</sup>	%	%	%		
0.001	1	.85	.81	.07	.04	4.9	3.9	1.0
	5		.69	.34	.20	18.3	14.5	3.9
	10		.60	.63	.38	29.0	22.5	6.5
0.005	1	11.04	10.98	1.14	.67	7.6	4.8	2.8
	4		8.47	4.56	2.79	23.3	14.4	9.0
	10		6.50	9.55	6.12	41.1	24.7	16.4
0.01	1	30.12	27.42	4.10	2.47	9.0	4.8	4.1
3.31	1 5		20.77	16.75	10.76	31.1	16.1	15.0
	10		16.18	28.06	18.97	46.3	23.4	22.9
0.02	1	77.82	69.72	10.48	6.40	10.4	4.6	5.8
	5		50.42	48.44	32.83	35.2	14.6	20.6
	10		37.54	77.70	56.24	51.8	20.8	30.9

- (a) =  $[MgS0_4^0]_0$ ,  $MgS0_4$  ion-pair concentration ir ure  $MgS0_4$  solution.
- (b) = [MgS0<sup>0</sup><sub>4</sub>]<sub>M</sub>, MgS0<sub>4</sub> ion-pair concentration in mixture.
- (c) = [NaS0-4]<sub>M</sub>, NaS0-4 ion-pair concentration in mixtu e.
- (d) = [MgCl<sup>+</sup>]<sub>M</sub>, MgCl<sup>+</sup> ion-pair concentration in mixture.
- (e) = Reduction in absorption due to ionic strength.
- (f) = Reduction in absorption due to ion-pairing.

TABLE II

Comparison of Experimental and Theoretically Derived F Values for 0.02 M MgSO<sub>4</sub> Mixtures with NaCl Added. The F values are those Calculated According to the Empirical Kurtze and Tamm equation.

Domosto	F	Dissociation Constants		
Remarks		K <sub>MaCI+</sub>	K <sub>NaSO4</sub>	k <sub>meso1</sub>
Kurtze and Tamm	.21			
Hsu	.129			
Predicted in this work	.134	.178	.1	.0062
Doubled dissociation constants of NaSO <sub>4</sub> and mgC7+	.093	.356	.2	.0062
No NaSO4 and MgCt	.052	100	100	.0062
No NaSO4	.081	.178	100	.0062
No MgCl+	.102	100	.1	.0062

TABLE III Comparison of Stoichiometric Activity Coefficients  $\gamma_{\pm} = \alpha f_{\pm}$  in This Paper with Measured Values

m.	This Paper	Robinson & Jones		Litzke & Stoughton	
		V.P.	F.P.		
06	261				
.05	.251				
.10	.192	.195	.195	.196	
.20	.144	.140	.142	.141	
.30	.122	.114	****	.115	
.40	.107	.0988		.100	
.50	.0972	.0882	.091	.089	
.6896			.081	****	
.70	.0836	.0747		.075	
.80	.0788	****		.071	
1.0	.0712	.0635	.067	.064	

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